

# Thermodynamics of liquid mixtures of acids: phase equilibria and excess molar enthalpies of acetic acid mixtures with active non-associating components

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(Received 11 March 1993; accepted 5 April 1993)

## Abstract

Vapour–liquid equilibria and excess molar enthalpies of binary solutions of acetic acid with water, 2-butanone, methyl acetate and ethyl acetate are calculated using the UNIQUAC associated-solution model, which takes into account the autodimerization of acetic acid and the heteroassociation of unlike molecules. Prediction of ternary liquid–liquid equilibria for the acetic acid + water + nonassociating component systems are demonstrated from the same model with only binary parameters. The calculated results agree well with the experimental values.

## LIST OF SYMBOLS

$A, A_1, A_2$	acid, acid monomer and acid dimer
$a_{JI}$	binary interaction parameter for J–I pair
AB	1:1 chemical complex involving acid and active component
B, $B_1$	nonassociating component and nonassociating component monomer
$B_{II}^F$	free contribution to second virial coefficient of component I
$C_{JI}, D_{JI}$	coefficients of eqn. (14)
$F$	objective function as defined by eqn. (22)
$H^E$	excess molar enthalpy
$h_A$	enthalpy of hydrogen bond formation for acid dimer
$h_{AB}$	enthalpy of complex formation between components A and B
$K_A$	equilibrium constant of acid dimer formation
$K_{AB}$	solvation constant between components A and B
$N$	number of experimental data points
$P$	total pressure

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$P_I^s$	saturated vapour pressure of pure component I
$q_I$	molecular geometric area parameter of pure component I
$R$	universal gas constant
$r_I$	molecular geometric volume parameter of pure component I
$T$	absolute temperature
$V$	true molar volume of acid mixture given by eqn. (10)
$V_A^\circ$	true molar volumes of pure acid given by eqns. (11)
$v_I^L$	pure liquid molar volume of component I
$x_I$	liquid-phase mole fraction of component I
$y_I$	vapour-phase mole fraction of component I
$y_{I_1}$	vapour-phase mole fraction of monomeric component I
$Z$	lattice coordinate number, here set as 10

#### *Greek letters*

$\gamma_I$	activity coefficient of component I
$\theta_I$	surface fraction of component I
$\sigma_P, \sigma_T, \sigma_x, \sigma_y$	standard deviations in pressure, temperature, liquid and vapour compositions, respectively
$\tau_{JI}$	coefficient as defined by $\exp(-a_{JI}/T)$
$\Phi_I$	segment fraction of component I
$\Phi_{I_1}$	monomer segment fraction of component I
$\Phi_{I_1}^\circ$	monomer segment fraction of pure acid given by eqn. (12)
$\phi_I$	fugacity coefficient of component I at $P$ and $T$
$\phi_I^s$	fugacity coefficient of pure component I at $P_I^s$ and $T$

#### *Subscripts*

A	acid
$A_1, A_2$	acid monomer and acid dimer
AB	binary 1:1 complex between components A and B
B	non-associating component
chem	chemical
I, J, K	components I, J and K
phys	physical

#### *Superscripts*

$^\circ$	pure liquid reference state
*	50°C

#### INTRODUCTION

The UNIQUAC associated-solution model has been successfully applied to describe vapour–liquid equilibria and excess molar enthalpies of alcanoic acid + hydrocarbon mixtures, under the assumption that the acid self-associates to form dimers in the vapour and liquid phases [1, 2]. The same

model has been extended to represent vapour–liquid equilibrium and excess molar enthalpy data for acid + alcohol mixtures [3].

In this paper, based on the UNIQUAC associated-solution model, we study the vapour–liquid equilibria and excess molar enthalpies of binary mixtures of acetic acid + water, +2-butanone, +methyl acetate and +ethyl acetate and the prediction of ternary liquid–liquid equilibria of acetic acid solutions including water and a non-associated component from binary parameters alone.

### SOLUTION MODEL

We assume that in the liquid phase acetic acid (A) forms cyclic dimers by autoassociation, and acetic acid and an active non-associating component (B) solvate to yield 1:1 chemical complexes. the equilibrium constants for self-association and solvation,  $K_A$  and  $K_{AB}$ , are defined by

$$\begin{aligned} K_A &= \frac{\Phi_{A_2}}{\Phi_{A_1}^2} \frac{1}{2} \quad \text{for } A_1 + A_1 = A_2 \\ &= K_A^* \exp \left[ -\frac{h_A}{R} \left( \frac{1}{T} - \frac{1}{T^*} \right) \right] \end{aligned} \quad (1)$$

$$\begin{aligned} K_{AB} &= \frac{\Phi_{AB}}{\Phi_{A_1} \Phi_{B_1}} \frac{1}{r_A + r_B} \quad \text{for } A_1 + B_1 = AB \\ &= K_{AB}^* \exp \left[ -\frac{h_{AB}}{R} \left( \frac{1}{T} - \frac{1}{T^*} \right) \right] \end{aligned} \quad (2)$$

where  $\Phi$  is the segment fraction,  $h_A$  the enthalpy of hydrogen bond for dimer formation,  $h_{AB}$  the enthalpy of complex formation and superscript \* denotes a reference temperature, here equal to 50°C.

### Binary systems

#### Activity coefficient

The UNIQUAC associated-solution model provides the following expressions of the activity coefficients for acetic acid (A) and the active non-associated component (B)

$$\begin{aligned} \ln \gamma_A &= \ln \left( \frac{\Phi_{A_1}}{\Phi_{A_1}^o} \right) + r_A \left( \frac{1}{V_A^o} - \frac{1}{V} \right) - \left( \frac{Z}{2} \right) q_A \left[ \ln \left( \frac{\Phi_A}{\theta_A} \right) + 1 - \frac{\Phi_A}{\theta_A} \right] \\ &\quad + q_A \left[ 1 - \ln \left( \sum_J \theta_J \tau_{JA} \right) - \sum_K \frac{\theta_K \tau_{AJ}}{\sum_K \theta_K \tau_{KJ}} \right] \end{aligned} \quad (3)$$

$$\begin{aligned} \ln \gamma_B &= \ln \left( \frac{\Phi_B}{x_B} \right) + 1 - \frac{r_B}{V} - \left( \frac{Z}{2} \right) q_B \left[ \ln \left( \frac{\Phi_B}{\theta_B} \right) + 1 - \frac{\Phi_B}{\theta_B} \right] \\ &\quad + q_B \left[ 1 - \ln \left( \sum_J \theta_J \tau_{JB} \right) - \sum_K \frac{\theta_K \tau_{BJ}}{\sum_K \theta_K \theta_{KJ}} \right] \end{aligned} \quad (4)$$

where  $Z$  is the lattice coordination number, here set as 10, and the segment fraction  $\Phi_I$ , the surface fraction  $\theta_I$ , the binary coefficient  $\tau_{JI}$  related to the binary interaction parameter  $a_{JI}$  are expressed by

$$\Phi_I = r_I x_I / \sum_J r_J x_J \quad (5)$$

$$\theta_I = q_I x_I / \sum_J q_J x_J \quad (6)$$

$$\tau_{JI} = \exp(-a_{JI}/T) \quad (7)$$

The monomer segment fractions of both components are simultaneously solved from eqns. (8) and (9).

$$\begin{aligned} \Phi_A &= \Phi_{A_1} + \Phi_{A_2} + \Phi_{AB} r_A / r_{AB} \\ &= \Phi_{A_1} + 2K_A \Phi_{A_1}^2 + K_{AB} \Phi_{A_1} \Phi_{B_1} r_A \end{aligned} \quad (8)$$

$$\begin{aligned} \Phi_B &= \Phi_{B_1} + \Phi_{AB} r_B / r_{AB} \\ &= \Phi_{B_1} + K_{AB} \Phi_{A_1} \Phi_{B_1} r_B \end{aligned} \quad (9)$$

where  $r_{AB} = r_A + r_B$  is assumed.

The true molar volume of the mixture is given by

$$\frac{1}{V} = \frac{\Phi_{A_1}}{r_A} (1 + K_A \Phi_{A_1}) + \frac{\Phi_{B_1}}{r_B} + K_{AB} \Phi_{A_1} \Phi_{B_1} \quad (10)$$

At pure acid state  $V_A^\circ$  and  $\Phi_{A_1}^\circ$  are given by eqns. (11) and (12)

$$\frac{1}{V_A^\circ} = \frac{1 - K_A \Phi_{A_1}^{\circ 2}}{r_A} \quad (11)$$

$$\Phi_{A_1}^\circ = [-1 + (1 + 8K_A)^{0.5}] / 4K_A \quad (12)$$

### *Excess molar enthalpy*

The excess molar enthalpy of the acid mixture is expressed as the sum of the chemical and physical contributions.

$$\begin{aligned} H^E &= H_{\text{chem}}^E + H_{\text{phys}}^E \\ &= h_A x_A K_A \left( \frac{\Phi_{A_1}^2}{\Phi_A} - \Phi_{A_1}^{\circ 2} \right) + \frac{h_{AB} K_{AB} \Phi_{A_1} \Phi_{B_1} r_A x_A}{\Phi_A} \\ &\quad - R \sum_I q_I x_I \frac{\sum_J \theta_J \frac{\partial \tau_{JI}}{\partial (1/T)}}{\sum_J \theta_J \tau_{JI}} \end{aligned} \quad (13)$$

The binary energy parameters are assumed to be linearly temperature

dependent.

$$a_{JI} = C_{JI} + D_{JI}(T - 273.15) \quad (14)$$

### Ternary systems

In a ternary mixture containing acid (A) and two active non-associating components (B and C), we assume additional complex formation between acid and component C.

$$\begin{aligned} K_{AC} &= \frac{\Phi_{AC}}{\Phi_{A_1}\Phi_{C_1}} \frac{1}{r_A + r_C} \quad \text{for } A_1 + C_1 = AC \\ &= K_{AC}^* \exp\left[-\frac{h_{AC}}{R}\left(\frac{1}{T} - \frac{1}{T^*}\right)\right] \end{aligned} \quad (15)$$

The monomer segment fractions,  $\Phi_{A_1}$ ,  $\Phi_{B_1}$  and  $\Phi_{C_1}$ , are given by simultaneous solution of the following mass balance equations:

$$\Phi_A = \Phi_{A_1} + 2K_A\Phi_{A_1}^2 + K_{AB}\Phi_{A_1}\Phi_{B_1}r_A + K_{AC}\Phi_{A_1}\Phi_{C_1}r_A \quad (16)$$

$$\Phi_B = \Phi_{B_1} + K_{AB}\Phi_{A_1}\Phi_{B_1}r_B \quad (17)$$

$$\Phi_C = \Phi_{C_1} + K_{AC}\Phi_{A_1}\Phi_{C_1}r_C \quad (18)$$

The true molar volume  $V$  of the ternary mixture is expressed by

$$\frac{1}{V} = \frac{\Phi_{A_1}}{r_A}(1 + K_A\Phi_{A_1}) + \frac{\Phi_{B_1}}{r_B} + K_{AB}\Phi_{A_1}\Phi_{B_1} + \frac{\Phi_{C_1}}{r_C} + K_{AC}\Phi_{A_1}\Phi_{C_1} \quad (19)$$

The activity coefficient of component C is obtained by changing the subscript B in eqn. (4) to the subscript C.

### CALCULATED RESULTS

Table 1 shows the molecular structural parameters of pure components,  $r$  and  $q$ , which were estimated according to the method of Vera et al. [4].

Vapour–liquid equilibrium data were reduced using the thermodynamic

TABLE 1  
Molecular structural parameters for pure components

Component	$r$	$q$	Component	$r$	$q$
Acetic acid	1.78	1.62	Methyl acetate	2.25	2.00
Benzene	2.56	2.05	Toluene	3.10	2.48
2-Butanone	2.60	2.28	Tetrachloromethane	2.71	2.37
Cyclohexane	3.18	2.55	Water	0.73	1.19
Ethyl acetate	2.79	2.43			

TABLE 2

Solvation parameters for binary mixtures

System (A + B)	$K_{AB}$ at 323.15 K	$-h_{AB}/\text{kJ mol}^{-1}$
Acetic acid + water	60	23.4
Acetic acid + 2-butanone	40	22.0
Acetic acid + ethyl acetate	40	20.5
Acetic acid + methyl acetate	40	20.5

relation

$$P\phi_I y_I = \gamma_I x_I \phi_I^s P_I^s \left[ \frac{v_I^L (P - P_I^s)}{RT} \right] \quad (20)$$

where  $P$  is the total pressure,  $\phi_I$  the fugacity coefficient of component I,  $y_I$  the vapour-phase mole fraction of component I,  $P_I^s$  the pure component vapour pressure taken from the original vapour–liquid equilibrium data set,  $v_I^L$  the pure-liquid molar volume estimated from the modified Rackett equation [5]. The fugacity coefficient  $\phi_I$  is calculated from the chemical theory of vapour imperfections [6].

$$\phi_I = \frac{y_{I_1}}{y_I} \exp\left(\frac{PB_{II}^F}{RT}\right) \quad (21)$$

where  $y_{I_1}$  is the vapour-phase monomer mole fraction of component I and  $B_{II}^F$  the free contribution to the second virial coefficient [7]. The association parameters of acetic acid were taken from Tamura and Nagata [1]:  $K_A = 14651.2$  at 50°C and  $-h_A = 44.5 \text{ kJ mol}^{-1}$ . The solvation parameters are shown in Table 2.

The computer program described by Prausnitz et al. [8] was used to seek an optimum set of the energy parameters by minimizing the object function.

$$F = \sum_{i=1}^N \left[ \frac{(P_i - \hat{P}_i)^2}{\sigma_P^2} + \frac{(T_i - \hat{T}_i)^2}{\sigma_T^2} + \frac{(x_{I_i} - \hat{x}_{I_i})^2}{\sigma_x^2} + \frac{(y_{I_i} - \hat{y}_{I_i})^2}{\sigma_y^2} \right] \quad (22)$$

where a circumflex denotes the most probable calculated value corresponding to each measured variable and the standard deviations of the measured values are: for pressure,  $\sigma_P = 1 \text{ Torr}$ ; for temperature,  $\sigma_T = 0.05 \text{ K}$ ; for liquid-phase mole fraction,  $\sigma_x = 0.001$ ; for vapour-phase mole fraction,  $\sigma_y = 0.003$ . Table 3 indicates the results of vapour–liquid equilibrium calculations and Figs. 1–4 compare the calculated results with the experimental values for some typical examples.

Table 4 lists the binary results of excess molar enthalpies. The coefficients,  $C_{JI}$  and  $D_{JI}$ , were obtained by minimizing the sum of the squares of the deviations between the experimental and calculated values.

TABLE 3  
Calculated results of binary vapour–liquid equilibrium data

System (A + B)	Temp./°C	No. of data points	Root-mean square deviations			Parameters/K		Reference
			$\delta p/\text{Torr}$	$\delta T/K$	$\delta x \times 10^3$	$\delta y \times 10^3$	$a_{AB}$	
Acetic acid + water	20	10	0.13	0.00	0.2	2.2	515.81	-244.68 9
	25	8	0.60	0.05	2.2	17.1	-29.06	72.47 9
	25	11	0.36	0.00	1.1	15.0	81.05	-62.13 10
	40	11	0.35	0.00	0.4	3.3	534.39	-262.06 9
	60	10	1.59	0.03	0.7	5.5	603.90	-300.70 11
	69.7	11	2.35	0.00	1.2	9.3	572.49	-294.46 11
	70	12	1.74	0.00	2.5	12.5	518.58	-282.59 10
	79.9	11	1.84	0.00	1.0	9.9	559.72	-300.32 11
	80	10	1.32	0.00	0.6	5.5	585.80	-307.80 9
	80.09	7	1.57	0.00	0.9	8.0	550.78	-291.86 9
	89.9	11	2.26	0.00	1.1	9.4	540.29	-300.79 11
Acetic acid + 2-butanone	68.51	8 <sup>a</sup>	2.25	0.00	1.2	6.5	-301.63	664.25 12
	78	9	5.47	0.01	2.7	5.2	-307.84	621.32 12
Acetic acid + ethyl acetate	65.01	11	1.20	0.04	1.7	13.7	-245.14	451.27 13
	≈65.18							
	72.94	11	1.77	0.07	3.1	22.2	-262.46	507.45 13
	≈73.08							
Water + benzene	25	MS <sup>b</sup>					546.62	1075.3 14
Water + 2-butanone	25	MS					21.44	379.69 14
Water + cyclohexane	25	MS					767.01	1490.5 14
Water + tetrachloromethane	25	MS					690.90	1453.4 14
Water + toluene	25	MS					539.46	1166.3 14
Water + ethyl acetate	30	MS					130.90	423.95 14

<sup>a</sup> One erroneous point rejected. <sup>b</sup> Mutual solubilities.

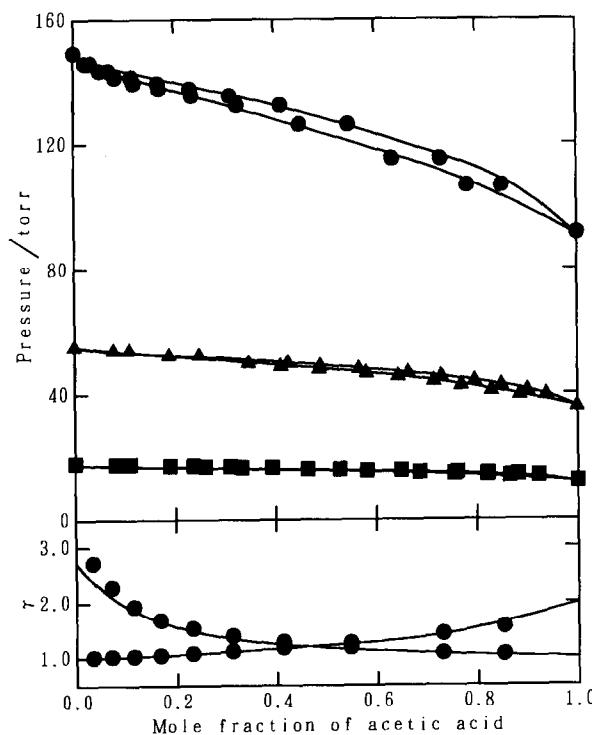


Fig. 1. Vapour-liquid equilibria for the acetic acid + water system. Calculated: —. Experimental: ■, 20°C [9]; ▲, 40°C [9]; ●, 60°C [11].

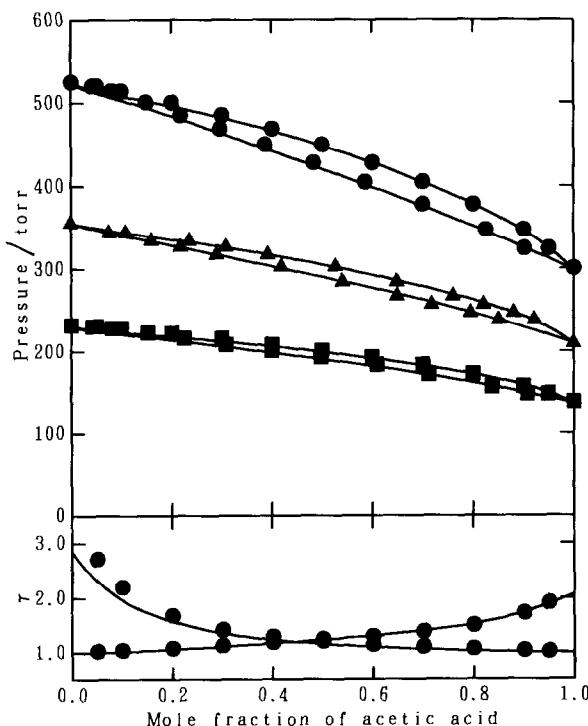


Fig. 2. Vapour-liquid equilibria for the acetic acid + water system. Calculated: —. Experimental: ■, 69.7°C [11]; ▲, 80°C [9]; ●, 89.9°C [11].

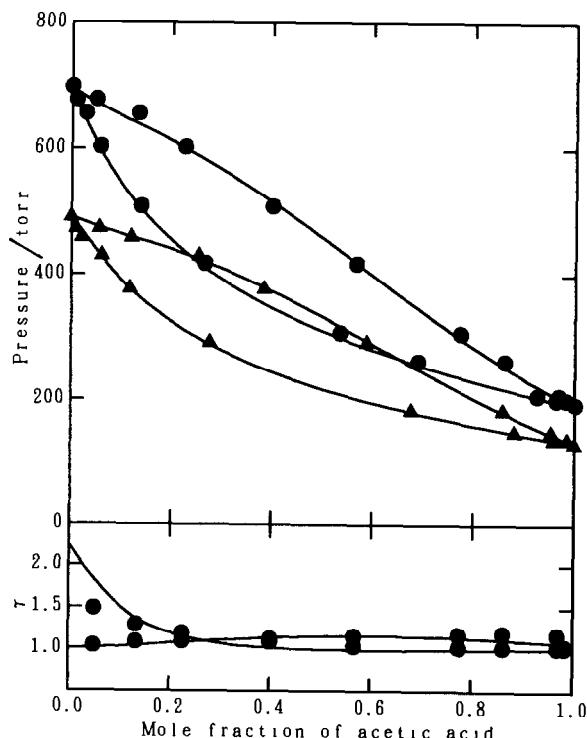


Fig. 3. Vapour-liquid equilibria for the acetic acid + 2-butanone system. Calculated: —. Experimental: ▲, 68.51°C [12]; ●, 78°C [12].

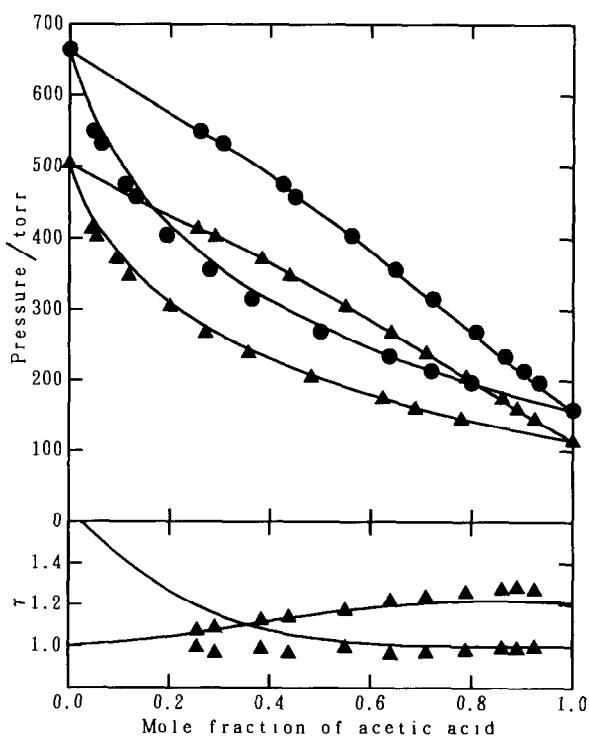


Fig. 4. Vapour-liquid equilibria for the acetic acid + ethyl acetate system. Calculated: —. Experimental: ▲, 65.01–65.18°C [13]; ●, 72.94–73.08°C [13].

TABLE 4  
Calculated results of binary excess enthalpy data

System (A + B)	Temp./°C	No. of data points	Parameters			Abs. arith. mean dev.	Reference	
			$C_{BA}/K$	$D_{BA}$	$C_{AB}/K$	$D_{AB}$		
Acetic acid + water	20	11	530.18	2.4578	253.33	-0.0934	2.83	15
Acetic acid + water	40	10	838.07	3.3492	327.43	0.1085	9.00	15
Acetic acid + 2-butanone	20	19	259.02	1.0128	457.27	1.7561	1.61	16
Acetic acid + ethyl acetate	19–26	9	352.40	1.6383	339.67	1.4212	1.48	15
Acetic acid + methyl acetate	35	13	124.53	0.6595	449.07	1.7307	3.07	15

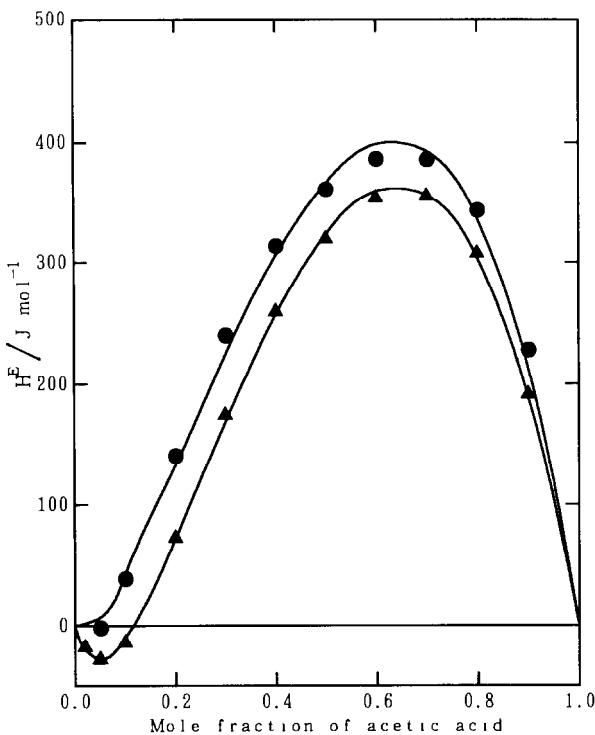


Fig. 5. Excess molar enthalpies for the acetic acid + water system. Calculated: —. Experimental: ▲, 20°C [15]; ●, 40°C [15].

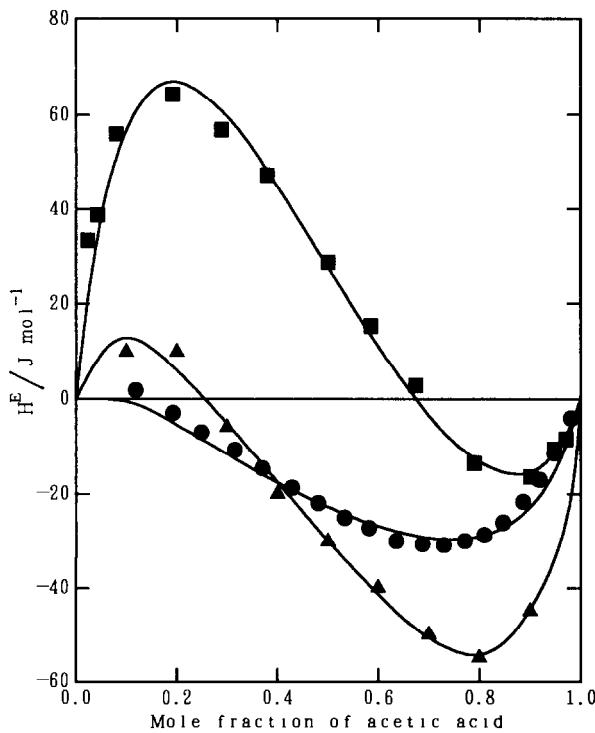


Fig. 6. Excess molar enthalpies for three acetic acid + organic compound systems. Calculated: —. Experimental: ●, acetic acid + 2-butanone at 20°C [16]; ▲ acetic acid + ethyl acetate at 19–26°C [15]; ■, acetic acid + methyl acetate at 35°C [15].

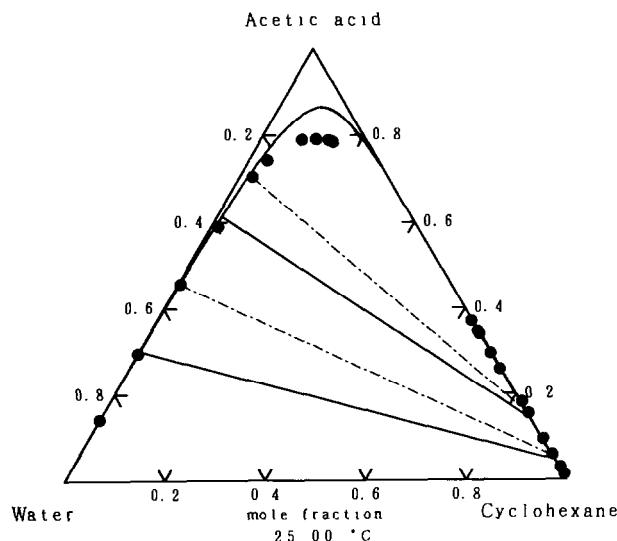


Fig. 7. Ternary liquid–liquid equilibria for the acetic acid + water + cyclohexane system at 25°C. Calculated: —. Experimental tie line [18]: ●—●.

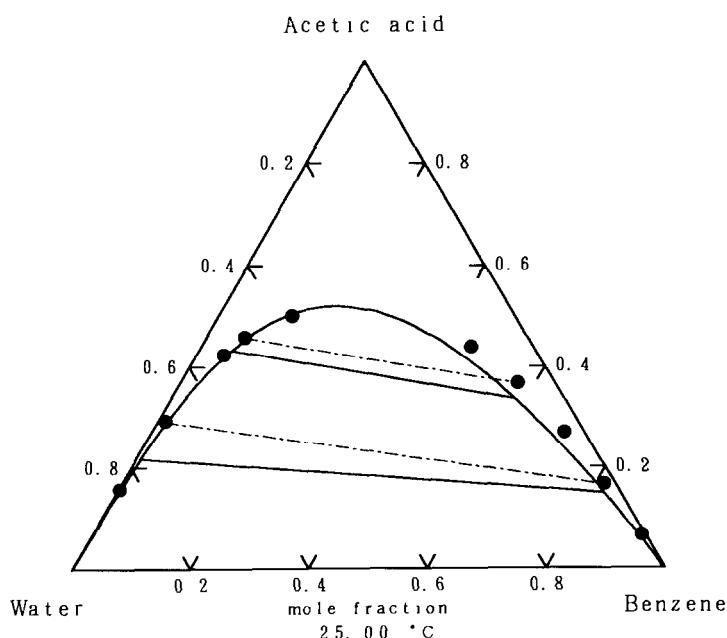


Fig. 8. Ternary liquid–liquid equilibria for the acetic acid + water + benzene system at 25°C. Calculated: —. Experimental tie line [18]: ●—●.

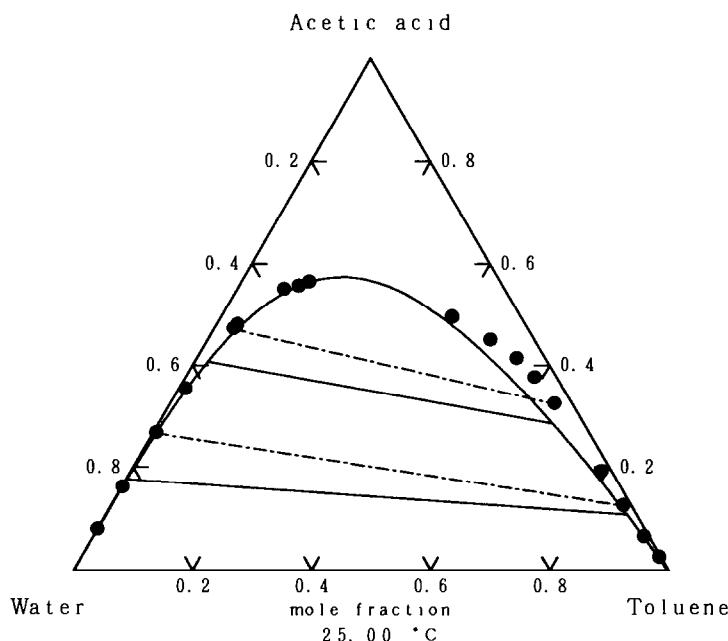


Fig. 9. Ternary liquid–liquid equilibria for the acetic acid + water + toluene system at 25°C.  
Calculated: —. Experimental tie line [18]: ●—●.

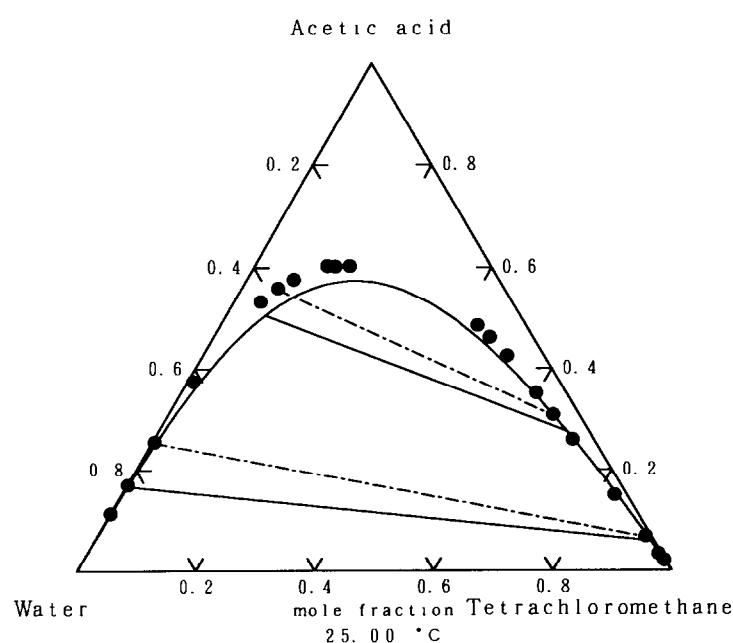


Fig. 10. Ternary liquid–liquid equilibria for the acetic acid + water + tetrachloromethane system at 25°C. Calculated: —. Experimental tie line [18]: ●—●.

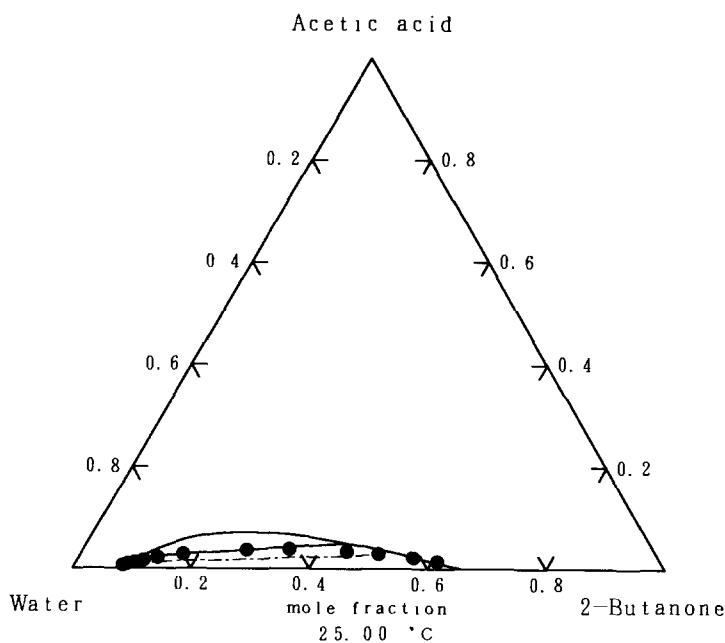


Fig. 11. Ternary liquid–liquid equilibria of the acetic acid + water + 2-butanone system at 25°C. Calculated: —. Experimental tie line [18]: ●—●.

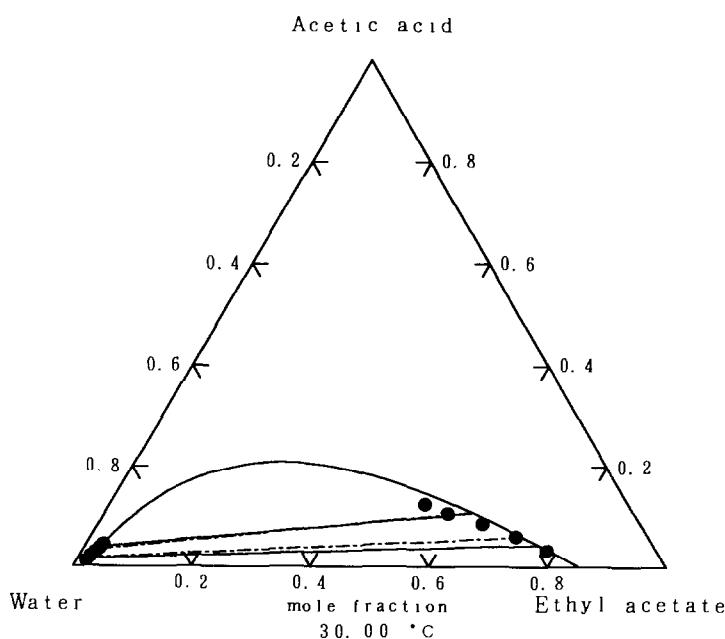


Fig. 12. Ternary liquid–liquid equilibria for the acetic acid + water + ethyl acetate at 30°C. Calculated: —. Experimental tie line [18]: ●—●.

The simplex method of Nelder and Mead [17] was used for this purpose. Figures 5 and 6 present the calculated and observed values of solutions of acetic acid with 2-butanone, ethyl acetate, methyl acetate and water.

Ternary prediction of liquid–liquid equilibrium was performed for six systems: acetic acid + water + cyclohexane, acetic acid + water + benzene, acetic acid + water + toluene, acetic acid + water + tetrachloromethane, acetic acid + water + 2-butanone and acetic acid + water + ethyl acetate. Figures 7–12 show that agreement is good.

We may conclude that the UNIQUAC associated-solution model is good in the correlation of vapour–liquid equilibrium and excess molar enthalpy data of binary acetic acid + active non-associating mixtures and could be used for the prediction of ternary liquid–liquid equilibrium data of solutions including acetic acid, water and one non-associated component.

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